

# Quantum Well Thermoelectric Devices

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## Abstract

This paper discloses the recent developments of high efficiency quantum well thermoelectrics at Hi-Z Technology, Inc.

The performance of the latest P type  $B_4C/B_9C$ - N-type Si/SiGe couple will be presented as well as data for the new N-type Si/SiC that will replace Si/SiGe and improve couple efficiency.

Preliminary calculations regarding the development of actual quantum well modules will be presented for power prediction. These modules can be used in future energy conversion system as well as air conditioning system designs.

Our current efforts to produce quantum well films more rapidly will be discussed.

## Introduction

Hi-Z Technology, Inc. (Hi-Z) is currently developing many different thermoelectric generator designs that are used to convert waste heat or heat sources directly to electricity. These include waste heat recovery from diesel trucks as well as automobiles and thermoelectric power generator including space application

Bismuth telluride based materials are presently used for power generation in remote locations, for example in deep space probes or direct conversion in general. Usage in direct conversion is conditional upon improvement in the efficiency of energy conversion from heat into electricity. The efficiency of thermoelectric energy conversion devices is strongly limited by the performance of the materials, which is normally measured in terms of a *Figure of Merit Z* (see next section).

Increasing the figure of merit of thermoelectric materials is difficult and basic properties of the materials. The breakthrough approach to increasing  $Z$  is to form compositionally modulated materials, mainly by QW confinement of carriers in the active layers in a multilayer film by adjacent barrier layers. The core concept is to enclose each electrically active layer by a material which has a band offset sufficient to form a barrier for the charge carriers. The major improvement in  $Z$  is expected to follow from an increased Seebeck coefficient that results from an increase in the density of states. There may also be a significant effect on the carrier mobility due to quantum confinement, so ideally there would be improvement in  $Z$  from the Seebeck coefficient, conductivity, and thermal conductivity. QW effects become significant only when the thickness of the active layer is small, below about  $200\text{\AA}$ . The effectiveness of QW confinement and its effect on the figure of merit depends on many factors such as the carrier concentration, which is temperature dependent.

In addition to QW confinement, improvement in  $Z$  may result from the periodicity of the multiple film structure on the thermal conductivity [1]. At low values of the thickness of individual layers, there may be interference with the propagation of phonon modes, and therefore a reduction in  $\kappa_{\perp}$ . The theory of this effect, and its application to both in-plane and through-plane thermal conductivity values, is now a subject of intense research and may

evolve into a field of engineered thermal transport semi-independently of thermoelectricity [2&3].

## Recent Advances

Hi-Z currently use conventional  $Bi_2Te_3$  alloys thermoelectric modules. The material in these modules has a value of  $ZT$  [figure of merit ( $Z$ ) times its mean absolute operation temperature ( $T$ )] of about 1. As shown in Figure 1, the value of  $ZT$  has hovered around 1 since the mid-1950s when semi-conductor materials were introduced into thermoelectric conversion. In the late 1990s new materials, including quantum well materials, started to increase the value of  $ZT$  to a out 4 with some promise that even higher values can be obtained as development continues.

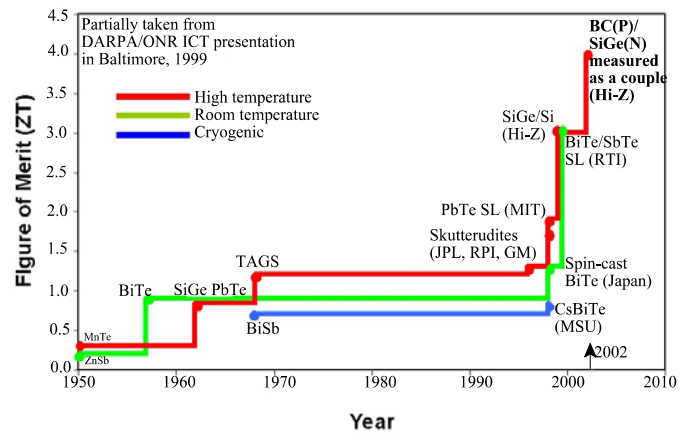


Figure 1: ZT Time Line

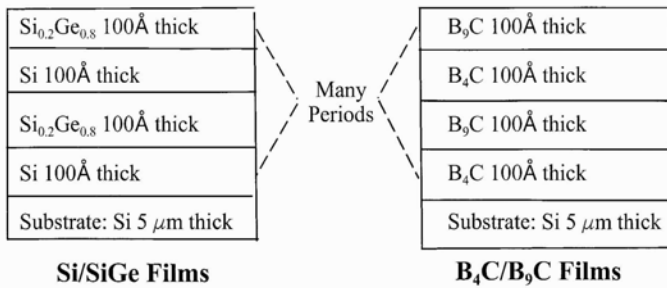
The figure of merit ( $Z$ ) for a thermoelectric material is obtained from its electric and thermal properties by

$$Z = \alpha^2 / \rho * \kappa$$

where  $\alpha$  is the Seebeck coefficient of the material,  $v/K$ ,  $\rho$  is its resistivity, ohm-cm, and  $\kappa$  is its thermal conductivity,  $W/cm K$ . Efforts to improve the value of  $Z$  for a bulk material often fails because as one increases  $\alpha$ , the values of  $\rho$  and/or  $\kappa$  usually also increase so that the resulting value of  $Z$  either remains the same or decreases. In 1992 Hicks and Duesselhouse [1] of MIT suggested that quantum wells should be a good candidate for thermoelectric energy conversion. This was confirmed in 1998 when Ghamaty and Elsner of Hi-Z [5] measured the thermoelectric properties of Si/SiGe quantum well films produced by both UCLA and the Navy for purposes other than thermoelectric energy conversion. Since then several investigators around the country have confirmed the improved thermoelectric properties of quantum well films.

Quantum well films have been made by several methods. The Navy films measured by Hi-Z were made by molecular beam epitaxy (MBE). Currently Hi-Z is making its films by magnetron sputtering. Several other methods of film fabrication are possible. While magnetron sputtering does not result in quantum well films with thermoelectric properties quite as good as films made by MBE, they can be made much more quickly and therefore have the potential for much lower cost.

- Si/SiGe: Multilayer Quantum Well film thermoelectrics
- P-type B<sub>4</sub>C/B<sub>9</sub>C: High temperature thermally stable multilayer Quantum Well films
- Si/SiC Quantum Well development underway to replace Si/SiGe for power (higher temperature) applications



**Figure 2:** Construction of Quantum Well Films

A quantum well film is formed by alternating thin (~100Å) layers of two materials with differing electron band gaps such as Si and SiGe as shown in Figure 2. When done correctly, all three of the thermoelectric properties improve, i.e.,  $\alpha$  increases and  $\rho$  and  $\kappa$  decrease. This results in a much improved Z and therefore an improved conversion efficiency ( $\eta$ ) because  $\eta$ , which is defined by the equation:

$$\eta = \frac{T_H - T_C}{T_H} \times \frac{M - 1}{M + \frac{T_C}{T_H}}$$

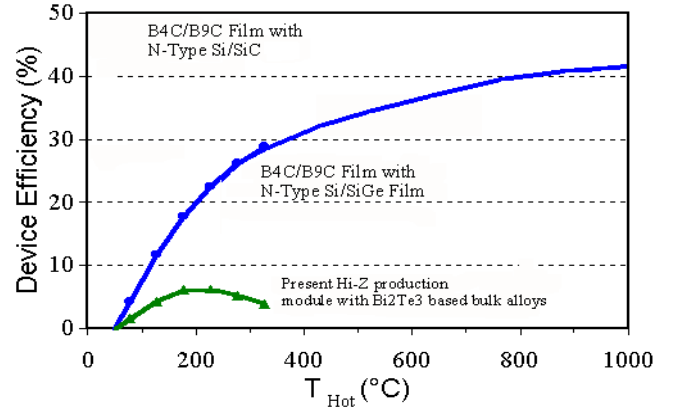
where the matching factor, M, is given by:

$$M = \sqrt{1 + \frac{Z}{2} (T_C + T_H)}$$

where  $T_C$  and  $T_H$  are respectively the cold and hot junction absolute temperatures. One will note that the first term of the efficiency equation is the Carnot efficiency.

Figure 3 is a graph of conversion efficiency as a function of ZT for various values of  $T_H$  and a value of  $T_C$  equal to 50°C. One can see that for even modest values of  $T_H$ , such as 250°C, and a value of  $ZT = 4$ , one can exceed a conversion efficiency of 20%.

A quantum well film useful in a thermoelectric module is made by making many periods of alternating 100Å layers. These layers are typically formed on a substrate such as silicon, which can remain as part of the film. If the substrate does remain, it becomes a parasitic loss in the system. This problem is discussed

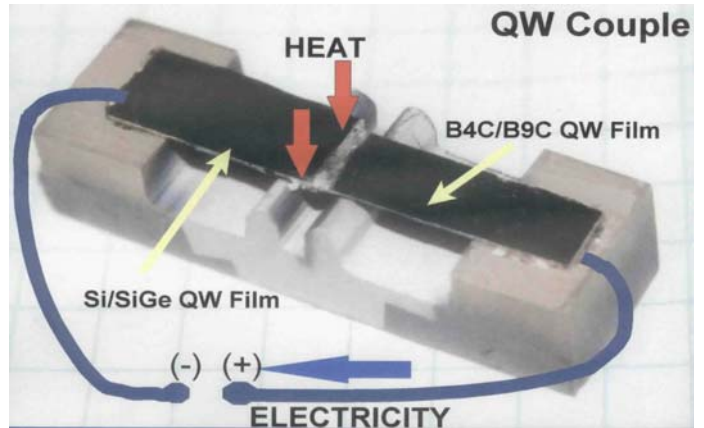


**Figure 3:** Calculated Couple Efficiency Versus Hot Side Temperature for B<sub>4</sub>C/B<sub>9</sub>C P-leg With a Si/SiGe or Si/SiC N-leg

later.

The first quantum well couple was reported in 2002 [6] and yielded 14% efficiency. Unfortunately it was accidentally destroyed by overheating.

A second quantum well couple was completed recently. This couple shown in Figure 4 consists of B<sub>4</sub>C/B<sub>9</sub>C for the P leg and Si/SiGe for the N leg. Both films were a total of 11 μm thick and were deposited on a 5 μm thick Si substrate. Figure 5 is a graph of the uncorrected module conversion efficiency as a function of the hot junction temperature and shows a conversion efficiency of over 14% at a  $T_H$  of 250°C. No corrections were made for heat loss through the leads, by radiation, or through the substrate.



**Figure 4:** Experimental Quantum Well Couple

Table 1 presents the raw data taken at a  $T_H$  of 250°C and  $T_C$  of 70°C both for the quantum well couple and a calibration couple made of bulk bismuth-telluride alloy couple taken on the same test rig.

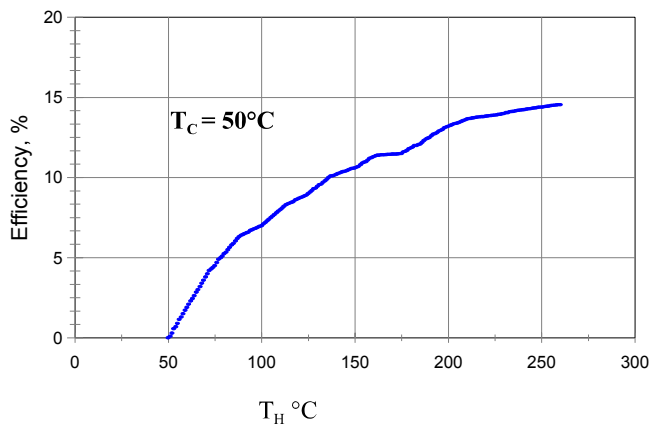
As previously mentioned, the substrate used will cause parasitic losses. Figure 6 presents a graph of the calculated quantum well conversion efficiency as a function of film thickness for films deposited on a 5 μm Si substrate for a  $T_H$  of 250°C and a  $T_C$  of 50°C. One can see that the curve appears to become asymptotic to about 25% efficiency for infinitely thick films. Also shown on the graph are the data from the test couple and that we plan to achieve of over 20% conversion efficiency at a film thickness of ~40 μm.

**Table 1. QW Device Raw Test Data for 11  $\mu\text{m}$  Thick  $\text{B}_4\text{C}/\text{B}_9\text{C}$  and  $\text{Si}/\text{SiGe}$  on 5  $\mu\text{m}$  Si at  $T_{\text{cold}} = 70^\circ\text{C}$  and  $T_{\text{hot}} = 250^\circ\text{C}$**

	Power Into Heater			Power Out From Couple			Efficiency
	Voltage	Current	Power	Voltage	Current	Power	
$\text{B}_4\text{C}/\text{B}_9\text{C}-\text{Si}/\text{SiGe}$	0.1413V	47.1 mA	6.657 mW	0.365 V	2.608 mA	0.952 mW	14.30%
Calibration: $\text{Bi}_2\text{Te}_3$ Alloys	2.510	0.836 A	2.098 W	0.034 V	3.15 A	0.107 W	5.10%

**Table 2. Thermoelectric Properties of Recently Fabricated Multi-layered QW  $\text{Si}/\text{SiC}$  Sputtered Film. Power number ( $\alpha^2/\rho$ ) of QW  $\text{Si}/\text{SiC}$  is  $\sim 250$  compare to bulk  $\text{Bi}_2\text{Te}_3$  power number of  $\sim 30$ .**

Samples at Room Temperature	Thickness ( $\text{\AA}$ )	$\rho$ , Resistivity ( $\text{m}\Omega\text{-cm}$ )	$\alpha$ , Seebeck Coefficient ( $\mu\text{V}/^\circ\text{C}$ )
03-01	400	2.15	-750
03-02	800	2.16	-755
03-03	1000	2.14	-745
03-04	1000	2.12	-753
03-05	1600	2.15	-754
03-06	1600	2.11	-758
03-07	1400	2.17	-760
03-08	1400	2.14	-750
03-09	1600	2.12	-752
03-10	1600	2.14	-755

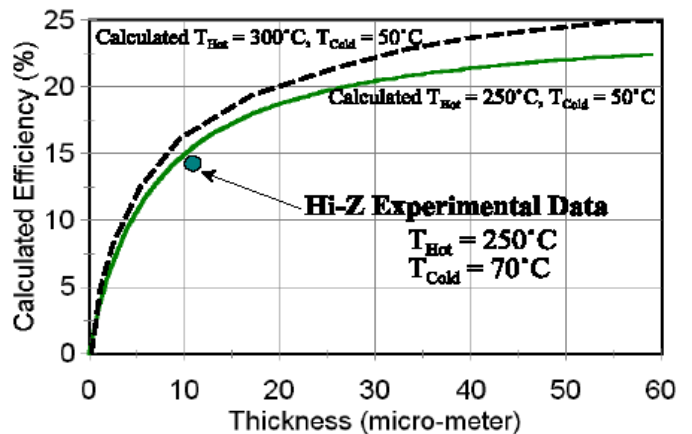


**Figure 5: Measured QW Couple Efficiency Versus Temperature**

Hi-Z has also been depositing quantum well films of  $\text{Si}/\text{SiC}$ . This is a N-type quantum well and can be used with the  $\text{B}_4\text{C}/\text{B}_9\text{C}$  P-type film for higher temperature applications. Table 2 presents the thermoelectric properties data obtained for several  $\text{Si}/\text{SiC}$  film samples of various thicknesses. These data were taken at room temperature.

**Cost**

Current bulk thermoelectric power modules are predicted to cost somewhat less than  $\$1/\text{Watt}$  when produced in high volumes. Similar quantum well modules are predicted to cost less than  $\$0.20/\text{Watt}$  in large volume production. The cost of cooling modules will be somewhat less on a per watt basis. The reason



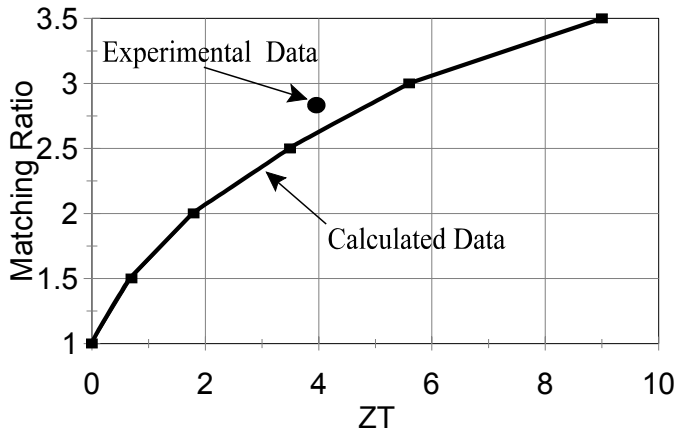
**Figure 6: Calculated Efficiency of a  $\text{B}_4\text{C}/\text{B}_9\text{C}-\text{Si}/\text{SiGe}$  Couple on a 5  $\mu\text{m}$  Si Substrate as a Function of Film Thickness**

for the predicted lower cost of quantum well devices is due both to their higher efficiency and the fact that they are made from lower cost raw materials than bulk thermoelectrics.

Hi-Z's current quantum well film production rate is quite low because of the size of our laboratory machine. Our current quantum well programs will allow us to obtain a much larger machine in the very near future. In addition, we are working with Pacific Northwest National Laboratories (PNNL) under the sponsorship of Department of Energy (DOE) to investigate production scale up of quantum well films. In addition, Hi-Z is also investigating alternative means, such as CVD, to fabricate quantum well films at higher rates.

## Discussion

Hi-Z has recently measured power and efficiency demonstrating a QW couple conversion efficiency of 14%. These measurements were made recently on a small couple that combined a multilayer QW of P type  $B_4C/B_9C$  with a QW of N type Si/SiGe. This couple operated between  $70^\circ\text{C}$  and  $250^\circ\text{C}$  and was fabricated on a  $5\mu\text{m}$  thick Si substrate with  $\sim 11\mu\text{m}$  QW film thickness. The 14% efficiency was calculated by dividing the power out of the couple by the power in. The 14% efficiency was obtained with no correction for any extraneous heat losses, such as through the Si substrate and the heater wires. The experimental set up also confirmed a known efficiency of  $\sim 5.5\%$  for  $\text{Bi}_2\text{Te}_3$  bulk alloys, assuring the data accuracy. The experimental data point and the predicted values agree quite well. A confirmation that these QW materials exhibit a much higher figure of merit than bulk alloys is that the maximum efficiency was achieved at a ratio of load resistance to QW couple resistance of  $\sim 2.6$  yielding a ZT of 4.1 at  $T \sim 250^\circ\text{C}$ , shown in Figure 7. The  $\text{Bi}_2\text{Te}_3$  bulk alloys meet their maximum efficiency at a resistance ratio of  $\sim 1.2$  when their ZT value is close to 1.



**Figure 7:** Matching ratio versus ZT for  $11\mu\text{m}$  thick QW film on  $5\mu\text{m}$  thick Si substrate.

In another separate experiment, the  $B_4C/B_9C$  film was used as a cooler creating a maximum temperature difference of  $\sim 45^\circ\text{C}$ . This temperature difference gives  $ZT \sim 3$  for  $T \sim 25^\circ\text{C}$ . For this experiment, the P-type  $B_4C/B_9C$  was joined to small Cu wire. The QW film was the same material and thickness as used in the couple mention above for the power generation systems, without the use of gases or moving parts.

## Acknowledgments

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